

Research Article

Optimal Constrained Stationary Intervention in Gene Regulatory Networks

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Received 11 January 2008; Accepted 9 April 2008

Recommended by Yufei Huang

A key objective of gene network modeling is to develop intervention strategies to alter regulatory dynamics in such a way as to reduce the likelihood of undesirable phenotypes. Optimal stationary intervention policies have been developed for gene regulation in the framework of probabilistic Boolean networks in a number of settings. To mitigate the possibility of detrimental side effects, for instance, in the treatment of cancer, it may be desirable to limit the expected number of treatments beneath some bound. This paper formulates a general constraint approach for optimal therapeutic intervention by suitably adapting the reward function and then applies this formulation to bound the expected number of treatments. A mutated mammalian cell cycle is considered as a case study.

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1. Introduction

One objective of genetic regulatory modeling is to design intervention strategies that affect the evolution of the gene activity profile of the network. Such strategies can be useful in identifying potential drug targets and treatment methods to alter network evolution in some desirable manner. The states of the network can be partitioned into two sets, desirable and undesirable, which correspond to functional cellular states, such as proliferation and apoptosis [1]. In biology, there are numerous examples where the (in)activation of one gene or protein can lead to a certain cellular functional state or phenotype. For instance, consider a stable cancer cell line borrowed from [2]. Without intervention, the cell cycle continues and cancerous cells proliferate with time. If the goal of the intervention is to push the cells into apoptosis, or programmed cell death, to stop the cell cycle one can use the p53 gene. The p53 gene is the most well-known tumor suppressor gene, encoding a protein that regulates the expression of several genes such as Bax and Fas/APO-1, which function to promote apoptosis [3, 4]. In cultured cells, extensive experimental results indicate that when p53 is activated, for example, in response to radiation, it leads to

cell growth inhibition or cell death [5]. The p53 gene is also used in gene therapy, where the target gene (p53 in this case) is cloned into a viral vector. The modified virus serves as a vehicle to transport the p53 gene into tumor cells to generate intervention [6, 7].

As this and many other examples suggest, it is prudent to use external variables to beneficially alter the evolution of gene regulatory networks. The design of intervention strategies that reduce the likelihood of states favorable to metastasis in cancerous cells has been recently studied by the systems biology community [2, 8]. In particular, regulatory intervention has been studied in the context of probabilistic Boolean networks (PBNs) [9]. These networks, which allow the incorporation of uncertainty into the inter-gene relationships, are essentially probabilistic generalizations of the standard Boolean networks introduced by Kauffman [10–12]. In a PBN, gene values are selected from a finite set of quantization levels. The values are updated synchronously at each updating epoch according to regulatory functions. The regulatory functions are allowed to change at time points selected by a binary switching random variable. This incorporates the effect of latent variables outside the model, whose behaviors influence regulation within the model. In

essence, the PBN is composed of a collection of networks; between switches it acts like one of the constituent networks. The PBN model also allows random perturbation of genes at each updating instant.

Under appropriate assumptions, a Markov chain models the dynamical behavior of a PBN [9, 13]. An optimal intervention strategy is developed based on the associated Markov chain. Methods have been proposed to devise effective intervention strategies. A one-time intervention has been designed based on first-passage times [14]. Dynamic programming can also be used to design optimal finite-horizon control policies [15]. Alternatively, Markov decision processes can be employed to find stationary intervention strategies that alter the steady-state distribution of the state space [16]. Recently, model-free methods have been introduced based on reinforcement learning [17] and mean first-passage times [18] to reduce the likelihood of visiting undesirable states in the long run.

Common to these approaches is a utility function that is to be maximized in order to reduce the aggregated probability of disease states. In reality, treatment options, for example, chemotherapy, cause collateral damages. For instance, consider a second example borrowed from [2]. A treatment based on estrogen is often used by women after menopause to alter their accelerated aging trend. The amount of estrogen received during treatment should not exceed a threshold, since an overdose may increase the chance of developing breast and ovarian cancers. While this phenomenon is not fully understood, it is conceivable that estrogen therapy may have side effects on gene regulation. Estrogen generates two types of complexes through binding to two classes of receptors. The generated complexes are transported into the nucleus to bind to the enhancer elements on the target genes with the help of a coactivator. The coactivator is also required for efficient transcriptional regulation by estrogen. This function in cooperation with a coactivator acts like a transcription factor, affecting target genes such as the PENK gene [19]. Two types of receptors are competing for binding to the estrogen received via treatment [20]. The first type of complex binds DNA better but performs less efficiently to bind the coactivator. On the other hand, the second type of complex binds the coactivator better but performs poorly when binding DNA. When the level of estrogen is below a threshold, there is no competition for DNA binding. Hence, the second type of complex binds DNA and activates the downstream target gene PENK, with the help of its coactivator. However, when the estrogen level is high, both types of complex exist at high concentrations, and the second type of complex binds the coactivator. Consequently, the level of coactivator available to complex type one drops, so the complex type two has a small chance to bind to DNA, and cannot activate the target gene. If the PENK gene plays a role in tumor suppression, for instance, then this could explain why high levels of estrogen have a tumorigenic effect. An appropriate treatment strategy mitigates this problem by bounding the expected number of treatments received by a patient and, as a consequence, limits the dose of estrogen.

Using constrained intervention methods, we seek an effective regulatory treatment that reduces the likelihood

of visiting undesirable gene-activity profiles, that is, state, in the long run while providing an upper bound on the expected number of interventions a patient can receive. Instead of introducing a single utility function whose maximization reduces the likelihood of entering undesirable states, we consider a situation where one type of utility is maximized while keeping the other cost function below a given threshold. Posed this way, the intervention problem can be viewed as a constrained Markov decision process.

In our framework, a gene regulatory network is modeled as a dynamical system in which decisions regarding treatment are taken sequentially. We wish to design an intervention strategy that selects treatments (actions) as a function of time and available information. For a given intervention strategy, the choice of treatments at different decision epochs may depend on the whole observed history. The choice of an intervention strategy will determine the evolution of the state of an intervened biological system in some probabilistic sense. The trajectories of the states together with the choice of treatments determine the expected utility in conjunction with the expected cost that we encounter. Hence, the proposed method enables us to design therapeutic intervention strategies by defining problem dependent constraints. Although various forms of constraints are plausible, hereafter, we focus on the expected number of treatments.

We provide the necessary background and formulate the problem of unconstrained intervention in a PBN as a Markov decision process in Section 2. The constrained intervention method is formulated in Section 3. As a numerical study, in Section 4, we consider a network obtained from the mammalian cell cycle with mutated phenotype. We design a constrained intervention strategy to hinder cell growth in the absence of growth factors, while keeping the expected number of interventions bounded. We investigate how the constrained intervention strategy performs in comparison to the unconstrained policy.

2. Unconstrained Optimal Intervention in Probabilistic Boolean Networks

A probabilistic Boolean network (PBN) consists of a sequence $V = \{x_i\}_{i=1}^n$ of n nodes, where $x_i \in \{0, \dots, d-1\}$, and a sequence $\{\mathbf{f}_l\}_{l=1}^k$ of vector-valued functions called predictor functions. In the framework of gene regulation, each element x_i represents the expression value of a gene. It is common to mix the terminology by referring to x_i as the i th gene. Each vector-valued function $\mathbf{f}_l = (f_{l1}, \dots, f_{ln})$ determines a constituent network of the PBN. The function $f_{li} : \{0, \dots, d^n - 1\}^n \rightarrow \{0, \dots, d^n - 1\}$ is a predictor of gene i , whenever network l is selected. The number of quantization levels is denoted by d . At each updating epoch, a decision is made whether to switch the constituent network. The switching probability q is a system parameter. If the network is not switched, then the PBN behaves like a fixed network and synchronously updates the values of all the genes according to the current predictor function. If the network is switched, then a predictor function is randomly selected

according to probability distribution $\{p_l\}_{l=1}^k$. After selecting the predictor function f_l , the values of genes are updated accordingly, that is, according to the network determined by f_l . We consider PBNs with perturbation, in which each gene may change its value with a small perturbation probability ϱ at each time unit.

Two quantization levels have thus far been used in practice. If $d = 2$ (binary), then the constituent networks are Boolean networks with 0 or 1 meaning OFF or ON, respectively. The case $d = 3$ (ternary) arises when we consider a gene to be down-regulated (0), up-regulated (2), or invariant (1). This situation commonly occurs with cDNA microarrays, where a ratio is taken between the expression values on the test channel (red) and the base channel (green). In this paper, we will develop the methodology for $d = 2$, so that gene values are either 0 or 1; however, the methodology is applicable to any finite number of levels.

The gene-activity profile (GAP) is an n -digit binary vector $\mathbf{x}(t) = (x_1(t), \dots, x_n(t))$ giving the expression values of the genes at time t , where $x_i(t) \in \{0, \dots, d - 1\}$. We note that there is a natural bijection between the GAP $\mathbf{x}(t)$ and its decimal representation, which takes values in $\mathcal{W} = \{0, 1, \dots, d^n - 1\}$.

In the presence of external controls, we suppose that the PBN has m binary control inputs, $\{c_i(t)\}_{i=1}^m$, which specify the interventions on control genes g_1, \dots, g_m . A control $c_i(t)$, which can take values 0 or 1 at each updating epoch t , specifies the action on the control gene g_i . The decimal bijection of the control vector, $u_{g_1, \dots, g_m}(t) \in \mathcal{C} = \{0, 1, \dots, 2^m - 1\}$, describes the complete status of all the control inputs. As in previous applications, we focus on a single control gene g_1 , which we label by g , possessing the control function $u_g(t) \in \mathcal{C} = \{0, 1\}$. The treatment alters the status of the control gene g , which can be selected among all the genes in the network. If the control at updating epoch t is on, $u_g(t) = 1$, then the state of the control gene g is toggled; if $u_g(t) = 0$, then the state of the control gene g remains unchanged.

Brun et al. showed that the dynamic behavior of a PBN can be modeled by a Markov chain [13]. In this case, system evolution for a single control gene g is represented by a stationary discrete-time equation:

$$z(t+1) = f(z(t), u_g(t), w(t)), \quad \text{for } t = 0, 1, \dots, \quad (1)$$

where state $z(t)$ is an element of the state-space $\mathcal{S} = \{(\xi, s) : \xi \in \{1, \dots, k\} \wedge s \in \{0, 1, \dots, d^n - 1\}\}$. The disturbance $w(t)$ is the manifestation of uncertainties in the PBN. It is assumed that both the gene perturbation distribution and the network switching distribution are independent and identical for all time steps t . Originating from a state z_1 , the successor state z_2 is selected randomly within the set \mathcal{S} according to the transition probability $p_{z_1 z_2}(u)$:

$$p_{z_1 z_2}(u) \stackrel{\Delta}{=} P(z(t+1) = z_2 \mid z(t) = z_1, u_g(t) = u), \quad (2)$$

for all z_1 and z_2 in \mathcal{S} , and for all u in \mathcal{C} . Gene perturbation insures that all the states in the Markov chain communicate with one another. Hence, the finite-state Markov chain has a unique steady-state distribution [21].

The problem of optimal intervention for PBNs is formulated as an unconstrained Markov decision process [16]. A reward-per-stage $r(z_1, u, z_2)$ is associated to each intervention in the system. In general, a reward-per-stage could depend on the origin state z_1 , the successor state z_2 , and the control input u . We assume that the reward-per-stage is stationary and bounded for all z_1, z_2 in \mathcal{S} , and u in \mathcal{C} . We define the average immediate reward in state z_1 , when control u is selected, by

$$\bar{r}(z_1, u) = \sum_{z_2 \in \mathcal{S}} p_{z_1 z_2}(u) r(z_1, u, z_2). \quad (3)$$

We consider the discounted formulation of the expected total reward. The discounting factor, $\alpha \in (0, 1)$, ensures the convergence of the expected total reward over the long-run [22]. In the case of cancer therapy, the discounting factor emphasizes that obtaining treatment at an earlier stage is favored over later stages. The normalized expected total discounted reward, given policy π_g , initial state i , and control gene g , is denoted by

$$\begin{aligned} J_{\pi_g}(i) \\ = (1 - \alpha) \lim_{N \rightarrow \infty} E \left\{ \sum_{t=0}^{N-1} \alpha^t r(z(t), \mu_g(i, t), z(t+1)) \mid z(0) = i \right\} \end{aligned} \quad (4)$$

A policy $\pi_g = \{\mu_g(i, 0), \mu_g(i, 1), \dots\}$ is a sequence of decision rules $\mu_g(i, t)$, for each updating epoch t acting on control gene g , given that the initial state is i . In general, a decision rule $\mu_g(i, t)$ at updating epoch t selects action $u_g(t)$ according to the history of the system as well as the current state. The history $h(t)$ at the updating epoch t is composed of the sequence of previous states and actions. If the history $h(t)$ is observed at the updating epoch t , then the decision rule $\mu_g(i, t)$ determines the probability of selecting action u conditioned on the history $h(t)$ and the current state $z(t)$. We denote the set of all such policies by Π_g , when gene g is selected as the control gene. The set $\Pi_g(M)$ is the subset of Markovian policies within the set of all policies Π_g defined above. A policy is Markovian if given the current state $z(t)$ the decision rule $\mu_g(i, t) = \mu_g(t)$ is independent of all the previous states and actions $h(t)$, and selects action u with probability $\mu_g(t, u \mid z(t))$ at decision epoch t . We denote the set of all stationary policies by $\Pi_g(S)$, where a stationary policy for control gene g is an admissible intervention strategy in $\Pi_g(M)$ of the form $\pi_g = \{\mu_g, \mu_g, \dots\}$. Here, μ_g denotes a time invariant decision rule. A stationary policy is also a deterministic policy if decision rule $\mu_g : \mathcal{S} \rightarrow \mathcal{C}$ is deterministic and time invariant for each updating epoch t . The set of all deterministic policies is represented by $\Pi_g(D)$.

Frequently, the discounted reward is defined without the normalizing constant $(1 - \alpha)$. This constant does not change the method and the solution of the intervention policy. However, using the normalizing constant has several advantages. First, this prevents the total reward from growing excessively for values of α close to one. Second, the use of the normalization constant provides an interesting interpretation for the total cost in the constrained intervention design. This will become clear in the later sections of the paper.

The vector \mathbf{J}_{π_g} of normalized expected total discounted rewards is called the value function. In an unconstrained intervention problem, we seek an admissible intervention strategy π_g^* that maximizes the value function for each initial state i , that is,

$$\pi_g^*(i) = \arg \max_{\pi_g \in \Pi_g} \mathbf{J}_{\pi_g}(i) \quad \forall i \in \mathcal{S}. \quad (5)$$

It is known that an optimal intervention strategy exists for the unconstrained discounted intervention problems, and it is given by the fixed-point solution of the Bellman optimality equation:

$$J^*(z_1) = \max_{u \in \mathcal{C}} \left[\bar{r}(z_1, u) + \alpha \sum_{z_2 \in \mathcal{S}} p_{z_1 z_2}(u) J^*(z_2) \right]. \quad (6)$$

Moreover, an optimal policy determined by the Bellman optimality equation is deterministic, and independent of the initial state i [22]. Standard dynamic programming algorithms can be used to find a fixed-point of the Bellman optimality equation.

3. Constrained Intervention in Probabilistic Boolean Networks

Cancer therapy may include the use of chemotherapy, radiation therapy, targeted gene therapy, and so forth. All of these treatment options are directed at killing or eradicating cancerous cells. Unfortunately, cancer treatments may also damage healthy cells. This results in complications and harmful side effects. It is therefore desirable to maintain the side effects of a treatment to a minimum. This goal can be achieved by enforcing an upper bound on the expected number of treatments a patient may receive during therapy. A deterministic intervention policy devised by solving the unconstrained optimization (5) reduces the chance of visiting undesirable states; however, this intervention policy does not provide a way to constrain the frequency of applying treatments within a prescribed intervention policy. To address this shortcoming, we impose an appropriate constraint on the optimization problem (5) by introducing constrained intervention in PBNs.

For the same reasons articulated in Section 2, we consider a discounted formulation to define both the objective reward function and constraint cost function. To restrict the frequency of applying intervention, we associate a cost-per-stage $c(z, u)$ to each state-action pair (z, u) in the constrained formulation. The set of all possible state-action pairs is denoted by $\mathcal{K} = \{(z, u) : z \in \mathcal{S}, u \in \mathcal{C}\}$. A cost-per-stage should be defined to appropriately reflect the constraint. Here, we bound the discounted expected number of interventions in the long run. Accordingly, the normalized expected total discounted cost of the constraint, given policy π_g , initial state i , and control gene g is denoted by

$$C_{\pi_g}(i) = (1 - \alpha) \lim_{N \rightarrow \infty} E \left\{ \sum_{t=0}^{N-1} \alpha^t c(z(t), \mu_g(i, t) \mid z(0) = i) \right\}. \quad (7)$$

Having the constrained cost function defined this way and the objective reward function as in (4), we can state the constrained intervention problem in a PBN as

$$\max_{\pi_g \in \Pi_g} \mathbf{J}_{\pi_g}(i), \quad \text{such that } C_{\pi_g}(i) \leq C_{\text{total}}, \quad (8)$$

where C_{total} is the upper bound on the discounted expected number of interventions in the long run, and i is the initial state.

We wish to find an optimal intervention policy π_g^* within the set of admissible policies Π_g (not just Markovian policies) that maximizes the value function while satisfying the constraint imposed on the discounted expected total cost. Interventions using policy π_g^* increase the time spent in desirable states, while limiting the discounted expected number of treatments. The intervention strategy is determined through the appropriate assignments of reward-per-stage and cost-per-stage to each state-action pair.

Given an arbitrary policy π_g and starting from initial state i , the state trajectories and selected actions over time are probabilistic. Our objective is to find the expectation of the number of times that state-action pairs $(z, u) \in \mathcal{K}$ with active intervention decision, $u = 1$, occur over the progression of the PBN. This value corresponds to the expected number of treatments in an intervention policy. To this end, we denote the probability that a state-action pair (z, u) in the set of all possible state-action pairs \mathcal{K} occurs at updating epoch t as

$$P_{\pi_g}(z(t) = z, u_g(t) = u \mid z(0) = i). \quad (9)$$

We further define the normalized discounted total expected time spent in the state-action pair (z, u) in the long run as

$$f_\alpha(i, \pi_g; z, u) \stackrel{\Delta}{=} (1 - \alpha) \lim_{N \rightarrow \infty} \sum_{t=0}^{N-1} \alpha^t P_{\pi_g}(z(t) = z, u_g(t) = u \mid z(0) = i), \quad (10)$$

for all $(z, u) \in \mathcal{K}$, where i is an initial state and π_g is a policy in Π_g . The set

$$f_\alpha(i, \pi_g) = \{f_\alpha(i, \pi_g; z, u) \mid (z, u) \in \mathcal{K}\} \quad (11)$$

denotes a probability measure over the set of state-action pairs \mathcal{K} . The numbers of states and actions of a PBN are finite, and the discounting factor α guarantees uniform convergence of (10). The set $f_\alpha(i, \pi_g)$ for any initial state i and policy π_g is called an *occupation measure* [23]. The occupation measure can be interpreted as the probability of occupying state-action pairs (z, u) in the long run, given that the PBN is initially in state i and policy π_g is used throughout.

The normalized discounted reward function (4) can be expressed as the expectation of the average immediate reward $\bar{r}(z, u)$ over the probability distribution defined in (9):

$$\begin{aligned} \mathbf{J}_{\pi_g}(i) = & (1 - \alpha) \lim_{N \rightarrow \infty} \sum_{t=0}^{N-1} \left\{ \alpha^t \sum_{(z,u) \in \mathcal{K}} [\bar{r}(z(t) = z, u_g(t) = u) \right. \\ & \left. \times P_{\pi_g}(z(t) = z, u_g(t) = u \mid z(0) = i)] \right\}. \end{aligned} \quad (12)$$

The normalized discounted reward function in (12) can be equivalently expressed as

$$\begin{aligned} J_{\pi_g}(i) &= \sum_{(z,u) \in \mathcal{K}} \left\{ (1 - \alpha) \lim_{N \rightarrow \infty} \sum_{t=0}^{N-1} [\alpha^t \bar{r}(z(t) = z, u_g(t) = u) \right. \\ &\quad \times P_{\pi_g}(z(t) = z, u_g(t) = u \mid z(0) = i)] \left. \right\}. \end{aligned} \quad (13)$$

Using definition (10) and probability measure (11), we can express the latest form of the normalized discounted reward (13) as the expectation of the average immediate reward with respect to the occupation measure:

$$J_{\pi_g}(i) = \sum_{(z,u) \in \mathcal{K}} f_\alpha(i, \pi_g; z, u) \bar{r}(z, u). \quad (14)$$

Similarly, we can express the normalized discounted objective cost corresponding to policy π_g as the expectation of the cost-per-stage with respect to the occupation measure:

$$C_{\pi_g}(i) = \sum_{(z,u) \in \mathcal{K}} f_\alpha(i, \pi_g; z, u) c(z, u). \quad (15)$$

Using (14) and (15), we can rewrite the constrained optimization problem (8) as

$$\begin{aligned} \max_{\pi_g \in \Pi_g} \sum_{(z,u) \in \mathcal{K}} f_\alpha(i, \pi_g; z, u) \bar{r}(z, u), \\ \text{such that} \\ \sum_{(z,u) \in \mathcal{K}} f_\alpha(i, \pi_g; z, u) c(z, u) \leq C_{\text{total}}. \end{aligned} \quad (16)$$

It is evident that the constraint in (16) prevents the discounted expected number of interventions in the long run from exceeding the upper-bound C_{total} if we assign the cost-per-stage for each state-action pair in \mathcal{K} as

$$c(z, u) = \begin{cases} 0, & \text{if } u = 0, z \in \mathcal{S}, \\ 1, & \text{if } u = 1, z \in \mathcal{S}. \end{cases} \quad (17)$$

In other words, using the definition of cost-per-stage in (17), the left side of the inequality constraint in (16) corresponds to the total discounted expected number of times that state-action pairs with active treatment, $u = 1$, occur under control policy π_g . Equivalently, we can interpret this as the discounted frequency of applying treatments given a therapeutic strategy.

Several solutions for the constrained optimization problem of (8) are presented in [24]. We next briefly present a method to solve this constrained Markov decision process using the equivalent problem formulation of (16). In [24], it is shown that the set of stationary policies $\Pi_g(S)$ is complete. In other words, if

$$L_U = \{f_\alpha(i, \pi_g) \mid \pi_g \in \Pi_g\} \quad (18)$$

denotes the set of all the occupation measures and

$$L_{U(S)} = \{f_\alpha(i, \pi_g) \mid \pi_g \in \Pi_g(S)\} \quad (19)$$

denotes the set of occupation measures generated by stationary policies only, then $L_U = L_{U(S)}$. Further, let $Q_\alpha(i)$ be defined as the set of vectors $\mathbf{x} = (x(1, 1), x(1, 2), \dots, x(2^n, 2^m))$ that satisfy

$$\begin{aligned} \sum_{(z,u) \in \mathcal{K}} x(z, u) (\mathbf{1}_{z=j} - \alpha p_{zj}(u)) &= (1 - \alpha) \mathbf{1}_{i=j} \quad \forall j \in \mathcal{S}, \\ x(z, u) &\geq 0 \quad \forall (z, u) \in \mathcal{K}, \end{aligned} \quad (20)$$

where $\mathbf{1}_x$ is indicator function, equaling one if x is true. If $\mathbf{x} \in Q_\alpha(i)$, then one can verify that $\sum_{(z,u) \in \mathcal{K}} x(z, u) = 1$ by summing the first constraint on \mathbf{x} in the definition of $Q_\alpha(i)$ over all $j \in \mathcal{S}$. Hence, the elements of any \mathbf{x} satisfying the constraints in (20) constitute a probability measure on \mathcal{K} .

It has been shown that $L_{U(S)} = \bar{L}_{U(D)}$, where $L_{U(D)} = \{f_\alpha(i, \pi_g) \mid \pi_g \in \Pi_g(D)\}$ and $\bar{L}_{U(D)}$ is the closed convex hull of deterministic policies [24]. Moreover, the closed convex hull of deterministic policies $\bar{L}_{U(D)}$ is equal to the closed polytope specified by $Q_\alpha(i)$. Hence, from the definition in (20) and the cost formulation (15), we can find an optimal policy that satisfies (16) by solving the following linear program:

$$\begin{aligned} \max_{\mathbf{x} \in \mathbb{R}^{|\mathcal{K}|}} \sum_{(z,u) \in \mathcal{K}} x(z, u) \bar{r}(z, u), \\ \text{such that} \\ \sum_{(z,u) \in \mathcal{K}} x(z, u) (\mathbf{1}_{z=j} - \alpha p_{zj}(u)) &= (1 - \alpha) \mathbf{1}_{i=j} \quad \forall j \in \mathcal{S}, \\ \sum_{(z,u) \in \mathcal{K}} x(z, u) c(z, u) &\leq C_{\text{total}}, \\ x(z, u) &\geq 0 \quad \forall (z, u) \in \mathcal{K}. \end{aligned} \quad (21)$$

This linear program is called the primal problem.

In [24], it is shown that an optimal stationary policy π_g^* of the constrained optimization problem (16) exists if and only if the primal problem (21) has a solution $\mathbf{x}^* = \{x^*(z, u) \mid (z, u) \in \mathcal{K}\}$. Moreover, an optimal solution of (21) uniquely determines an optimal stationary policy π_g^* . An optimal stationary policy, π_g^* , thus selects action u at state z with probability:

$$\pi_g^*(z, u) = \frac{x^*(z, u)}{\sum_{u \in \mathcal{C}} x^*(z, u)}. \quad (22)$$

We should point out that the optimal policy devised by (22) is not necessarily a deterministic policy, in contrast to a policy that maximizes reward function (4) without limitations.

Depending on the utilized numerical method, the computational complexity of finding a solution for the linear program in (21) varies. It is known that the complexity of the interior-point method increases polynomially with the number of states in \mathcal{K} , where the exponent of the complexity polynomial is not large [25]. Moreover, it is known that the number of iterations required for the numerical method to converge is in the order of $O(\log(1/\epsilon))$, where ϵ is the accuracy of the outcome of the numerical method. Here,

the size of \mathcal{K} increases exponentially with the number of genes n and the number of controls m in the PBN model with control. The goal, in the application of interest, is not to model fine-grained molecular interactions among a host of genes, but rather to model a limited number of genes, typically with very coarse quantization, whose regulatory activities are significantly related to a particular aspect of a specific disease. Hence, the proposed method is easily up to the task of handling the limited size networks with which we are dealing.

4. Constrained Intervention in a Mammalian Cell-Cycle Network

In this section, we construct a PBN that is a probabilistic version of the Boolean model for the mammalian cell cycle regulation proposed in [26]. This PBN postulates the mammalian cell cycle with a mutated phenotype. Our proposed constrained intervention method is then applied with various bounds on the frequency of applying treatments; the therapeutic policy seeks to hinder cell growth in the absence of growth factors.

During the late 1970s and early 1980s, yeast geneticists identified the cell-cycle genes encoding for new classes of molecules, including the cyclins (so-called because of their cyclic pattern of activation) and their cyclin dependent kinases (cdks) partners [26]. Our model is rooted in the work of Fauré et al., who have recently derived and analyzed the Boolean functions of the mammalian cell cycle [26]. The authors have been able to quantitatively reproduce the main known features of the wild-type biological system as well as the consequences of several types of mutations. Mammalian cell division is tightly controlled. In a growing mammal, the cell division should coordinate with the overall growth of the organism. This coordination is controlled via extra-cellular signals. These signals indicate whether a cell should divide or remain in a resting state. The positive signals, or growth factors, instigate the activation of Cyclin D (CycD) in the cell.

The key genes in this model are CycD, retinoblastoma (Rb), and p27. Rb is a tumor-suppressor gene. This gene is expressed in the absence of the cyclins, which inhibit Rb by phosphorylation. Whenever p27 is present, Rb can be expressed even in the presence of CycE or CycA. Gene p27 is active in the absence of the cyclins. Whenever p27 is present, it blocks the action of CycE or CycA. Hence, it stops the cell cycle.

The preceding explanation represents the wild-type cell-cycle model. Following one of the proposed mutations in [26], we assume p27 is mutated and its logical rule is always zero (OFF). In this cancerous scenario, p27 can never be activated. This mutation introduces a situation where both CycD and Rb might be inactive. As a result, in this mutated phenotype, the cell cycles in the absence of any growth factor. In other words, we consider the states in which both Rb and CycD are down-regulated as “undesirable states,” when p27 is mutated. Table 1 summarizes the mutated Boolean functions.

TABLE 1: Mutated boolean functions of mammalian cell cycle.

Product	Predictors
CycD	Input
Rb	$(\overline{\text{CycD}} \wedge \overline{\text{CycE}} \wedge \overline{\text{CycA}} \wedge \overline{\text{CycB}})$
E2F	$(\overline{\text{Rb}} \wedge \overline{\text{CycA}} \wedge \overline{\text{CycB}})$
CycE	$(\text{E2F} \wedge \overline{\text{Rb}})$
CycA	$(\text{E2F} \wedge \overline{\text{Rb}} \wedge \overline{\text{Cdc20}} \wedge (\overline{\text{Cdh1}} \wedge \overline{\text{Ubc}})) \vee (\text{CycA} \wedge \overline{\text{Rb}} \wedge \overline{\text{Cdc20}} \wedge (\overline{\text{Cdh1}} \wedge \overline{\text{Ubc}}))$
Cdc20	CycB
Cdh1	$(\overline{\text{CycA}} \wedge \overline{\text{CycB}}) \vee (\text{Cdc20})$
Ubc	$(\overline{\text{Cdh1}}) \vee (\text{Cdh1} \wedge \text{Ubc} \wedge (\text{Cdc20} \vee \text{CycA} \vee \text{CycB}))$
CycB	$(\overline{\text{Cdc20}} \wedge \overline{\text{Cdh1}})$

The Boolean functions in Table 1 are used to construct the PBN model for the cell cycle. To this end, we assume that the extra-cellular signal to the cell-cycle model is a latent variable. The growth factor is not part of the cell, and its value is determined by the surrounding cells. The expression of CycD changes independently of the cell’s content and reflects the state of the growth factor. Depending on the expression status of CycD, we obtain two constituent Boolean networks for the PBN. The first constituent Boolean network is determined from Table 1 when the value of CycD is equal to zero. Similarly, the second constituent Boolean network is determined by setting the variable of CycD to one. To completely define the PBN, the switching probability, the perturbation probability, and the probability of selecting each constituent Boolean network have to be specified. We assume that these are known. Here, we set the switching probability and the perturbation probabilities equal to 0.01 and 0.001, respectively, and the two constituent Boolean networks are equally likely.

According to Table 1, the mutated cell-cycle’s PBN consists of nine genes: CycD, Rb, E2F, CycE, CycA, Cdc 20, Cdh 1, UbcH 10, and CycB. The above order of genes is used in the binary representation of the states, with CycD as the most significant bit and CycB as the least significant bit. This order of genes in the states facilitates the presentation of our results and does not affect the computed control policies. Here, the set $\mathcal{S} = \{0, \dots, 511\}$ denotes the decimal bijection of gene-activity profiles when the above gene order is used for presentation

Preventing the states with simultaneously down-regulated CycD and Rb as our objective, we apply the constrained intervention method described in Section 3 to the constructed PBN with various bounds on the frequency of applying control in a policy. We only consider a single control, $u \in \mathcal{C} = \{0, 1\}$. If the control is high, $u = 1$, then the state of the control gene is reversed; if $u = 0$, then the state of the control gene remains unchanged. The control gene can be any of the genes in the model except CycD.

We assume that the reward of the states with down-regulated Rb and CycD is lower than those for the states in which these two genes are not simultaneously down-regulated. We also consider the cost of applying a control

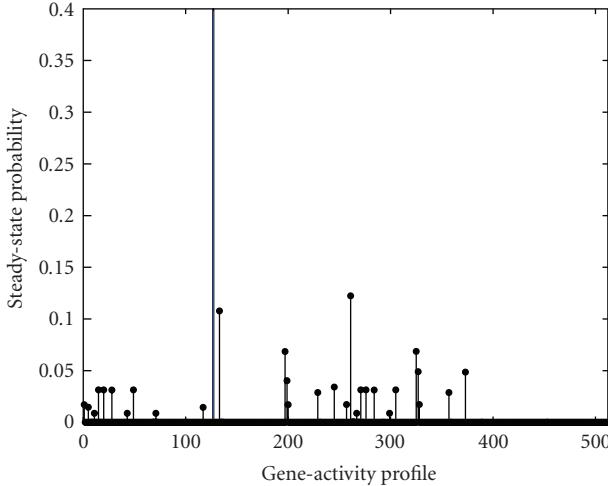


FIGURE 1: The steady-state probability of gene-activity profile of the PBN associated with the mammalian cell-cycle network before intervention. The vertical line separates the undesirable gene-activity profiles from the desirable ones.

action, which reduces the reward of each state. We postulate the following rate-of-reward function:

$$r(z, u) = \begin{cases} 10, & \text{if } u = 0, (\text{CycD}, \text{Rb}) \neq (0, 0) \text{ in } z, \\ 1, & \text{if } u = 0, (\text{CycD}, \text{Rb}) = (0, 0) \text{ in } z, \\ 9, & \text{if } u = 1, (\text{CycD}, \text{Rb}) \neq (0, 0) \text{ in } z, \\ 0, & \text{if } u = 1, (\text{CycD}, \text{Rb}) = (0, 0) \text{ in } z. \end{cases} \quad (23)$$

We select an arbitrary rate of reward; however, the reward and control cost are selected so that applying the control to prevent the undesirable states is preferable in comparison to not applying control and remaining in an undesirable state. In practice, the reward values have to capture the benefits and costs of the intervention and the relative preference of the states. They have to be set in conjunction with physicians according to their clinical judgement. Although this is not feasible within the domain of current medical practice, we do believe that such an approach will become increasingly mainstream once engineering approaches are demonstrated to yield significant benefits in translational medicine. Assuming the preceding rate-of-reward function, we can compute control policies for the PBN associated to the cell-cycle network according to various constraints.

Figure 1 depicts the steady-state distribution of the gene-activity profile when there is no intervention. Per Figure 1, in this PBN, the aggregated probability of the gene-activity profiles with simultaneously down-regulated CycD and Rb is close to 0.2. In other words, the model predicts that the mutated cell-cycle will be in the cancerous gene-activity profiles 0 to 127 nearly 20% of its time in the long run.

We define ΔP to be the percentage change in the aggregated probability of undesirable gene-activity profiles with simultaneously down-regulated CycD and Rb with and without intervention. As a performance measure, ΔP indicates the percentage of the reduction in the likelihood of cancerous situations in the long run.

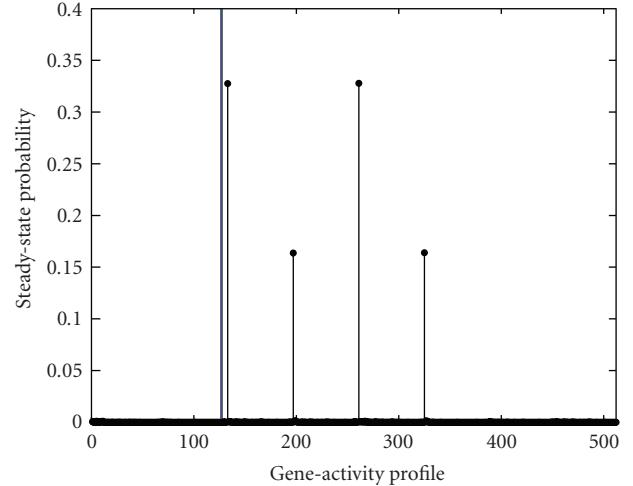


FIGURE 2: The steady-state probability of gene-activity profile of the PBN associated with the mammalian cell-cycle network after intervention using Rb as the control gene, when the frequency of applying control is unconstrained, $C_{\text{total}} = 1.0$. The vertical line separates the undesirable gene-activity profiles from the desirable ones.

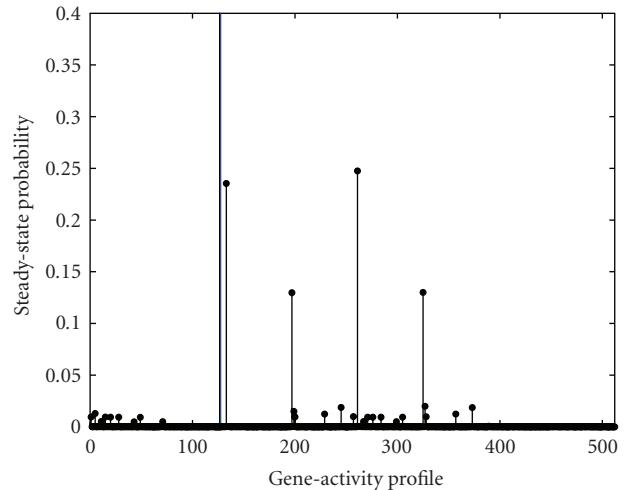


FIGURE 3: The steady-state probability of gene-activity profile of the PBN associated with the mammalian cell-cycle network after intervention using Rb as the control gene, when the frequency of applying control is upper bounded by $C_{\text{total}} = 0.1$. The vertical line separates the undesirable gene-activity profiles from the desirable ones.

If we assume that we can alter the expression level of any gene in the network as a therapeutic method, then it is natural to ask which gene should be used to alter the behavior of the model. To this end, we find a constrained intervention policy for each gene in the network using the intervention method explained in Section 3, while limiting the expected number of times a control can be applied. First, we assume that the PBN's initial state is the undesirable gene-activity profile with the highest probability in the steady-state distribution of gene-activity profiles prior to

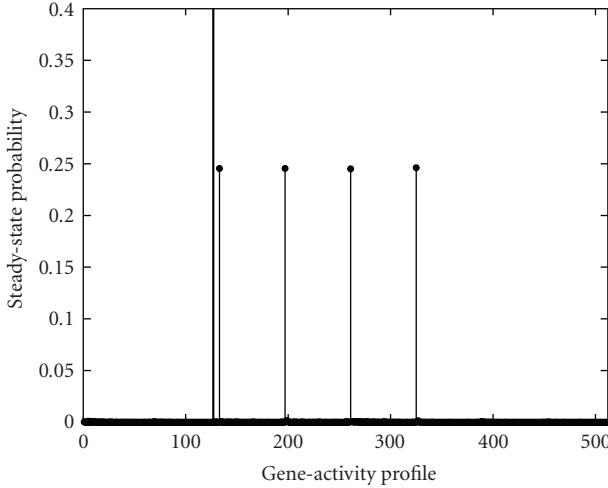


FIGURE 4: The steady-state probability of gene-activity profile of the PBN associated with the mammalian cell-cycle network after intervention using E2F as the control gene, when the frequency of applying control is unconstrained, $C_{\text{total}} = 1.0$. The vertical line separates the undesirable gene-activity profiles from the desirable ones.

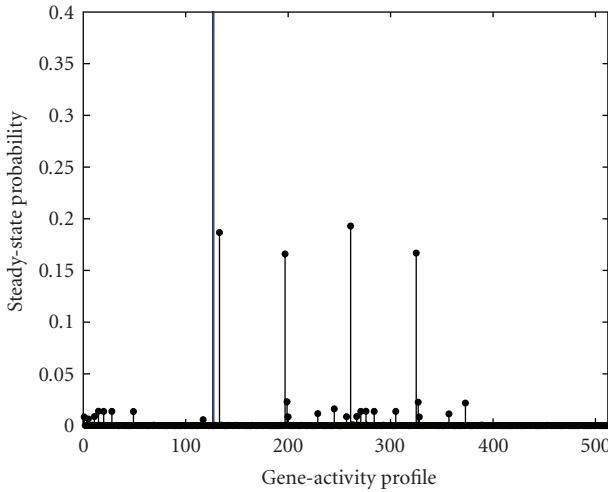


FIGURE 5: The steady-state probability of gene-activity profile of the PBN associated with the mammalian cell-cycle network after intervention using E2F as the control gene, when the frequency of applying control upper bounded by $C_{\text{total}} = 0.1$. The vertical line separates the undesirable gene-activity profiles from the desirable ones.

intervention. Table 2 lists the value of ΔP corresponding to each gene in the network. Here, we vary the upper bound on the frequency of applying intervention and find the corresponding constrained policies.

Among all the genes, Rb offers the best performance when control can be applied without any constraint, based strictly on maximization of the reward function, $C_{\text{total}} = 1$. After applying the unconstrained control policy designed for Rb, the aggregated probability of undesirable gene-activity profiles is significantly altered (see Figure 2). To

avoid the undesirable gene-activity profiles, we utilize the intervention strategy devised by the proposed method in Section 3 for the case when there is no bound on the expected number of treatments. In this scenario, let us assume that the gene-activity profile at a decision epoch indicates that $\text{CycD} = 0$, $\text{Rb} = 1$, $\text{E2F} = 1$, $\text{CycE} = 1$, $\text{CycA} = 0$, $\text{Cdc20} = 0$, $\text{Cdh1} = 1$, $\text{UbcH10} = 0$, and $\text{CycB} = 0$. The devised stationary intervention strategy, which is a mapping from the gene-activity profile to the action set \mathcal{C} , indicates that, for the observed gene-activity profile, the value of control gene Rb should be toggled with probability one. Consequently, we should use an appropriate inhibitor to forcefully down regulate the control gene Rb. Hence, the gene-activity profile would be forced from $(0, 0, 1, 1, 0, 0, 1, 0, 0)$ to $(0, 1, 1, 1, 0, 0, 1, 0, 0)$ after this intervention. Although the techniques to implement such a policy, that is, effectively altering the expression of gene Rb, using its enhancers and inhibitors, may not be fully understood within the domain of current medical practice, almost surely these techniques will have detrimental side effects. The constrained stationary intervention designed by the proposed procedure enables us to restrict the expected number of such interventions a patient may receive during therapy. Hence, we could accordingly adjust our intervention strategy when the side effects of drugs effecting the regulation of gene Rb are known.

Figure 3 indicates that by using a constrained stationary intervention policy for the control gene Rb we can reduce the aggregated probability of the undesirable states to less than 12%, while restricting the number of interventions to at most 10%. We could translate this to restrict the dose of prescribed drugs once knowledge of their side effects is available. If we only wish to limit the expected number of applied interventions to less than 20%, then we can reduce the chance of the cancerous gene-activity profiles by 98%.

According to Table 2, intervention policies based on gene E2F performs almost as well as Rb when the constraint is not too tight, $C_{\text{total}} \geq 0.2$. This suggests that, given the side effects of treatments, we may need to consider alternative control genes. The steady-state probability distributions of gene-activity profiles after intervention based on E2F are presented in Figures 4 and 5.

Comparing Figures 2 and 4, one can observe that although the final performances of intervening based on these two genes are close, the probability mass of the most probable gene-activity profiles after intervention with Rb differs from the one in E2F-based intervention. This observation suggests that one should utilize the systematic analysis along with experimental studies to obtain more effective lever points.

The results of Table 2 indicate that some genes are more sensitive to the bound on the frequency of control. Relaxing the constraint will not improve the result of intervention when the gene UbcH10 is selected as the control gene. It is simply not an effective lever point. Genes CycB and Cdc20 perform relatively well for tightly constrained intervention policies but relaxing the limitation on the expected number of treatments does not significantly improve the performance of the policies based on these genes.

TABLE 2: The ΔP for the intervention strategy based on various control genes and various constraint bounds.

Control gene	C_{total}									
	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
Rb	61.96	98.32	98.33	98.33	98.33	98.33	98.34	98.34	98.34	98.34
E2F	57.43	97.36	98.00	98.00	98.00	98.01	98.01	98.02	98.02	98.02
CycE	28.37	28.41	28.41	28.44	28.44	28.46	28.46	28.47	28.49	28.51
CycA	16.56	16.59	16.60	16.61	16.62	16.64	16.65	16.65	16.69	16.69
Cdc20	39.15	41.44	41.47	41.48	41.48	41.50	41.51	41.52	41.53	41.61
Cdh1	27.55	40.58	41.51	41.56	41.56	41.57	41.62	41.62	61.63	41.65
UbcH10	6.49	6.50	6.52	6.56	6.57	6.59	6.61	6.64	6.66	6.69
CycB	39.33	41.85	41.86	41.89	41.91	41.92	41.92	41.96	41.99	41.99

Furthermore, if we do not assume that the PBN's initial state is the undesirable gene-activity profile with the highest probability in the steady-state distribution of gene-activity profiles prior to intervention but instead initialize the PBN from an arbitrary undesirable gene-activity profile, we observe that the policies are robust to the initial state unless the constraint is too tight. For $C_{\text{total}} \geq 0.2$, the values of ΔP do not alter significantly; the performance of the intervention policy varies more for different initial gene-activity profiles when the constraint is tight, $C_{\text{total}} = 0.1$.

5. Conclusion

We have formulated the constrained intervention method in probabilistic Boolean networks and demonstrated that one can reduce the likelihood of a subset of undesirable states while bounding the expected number of interventions in a therapeutic strategy using the proposed method. We have considered a mutated mammalian cell-cycle network in which the cell growth does not stop in the absence of growth factors. We have then utilized the proposed intervention method to design constrained intervention policies to influence the dynamics of the PBN constructed for the mutated mammalian cell cycle. The goal of intervention is to reduce the chance of undesirable cell proliferation in the long run, while maintaining a bound on the expected number of interventions. The presented numerical studies strongly suggest that constrained intervention can effectively alter the dynamics of the cell-cycle model. Various control genes can be considered given different constraints. The most effective control gene may vary depending on the restrictions imposed on the intervention policies.

Acknowledgments

This work was supported in part by the National Science Foundation (ECS-0355227, CCF-0514644, and ECCS-0701531), the National Cancer Institute (R01 CA-104620 and CA-90301), and the Translational Genomics Research Institute.

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Special Issue on Network Structure and Biological Function: Reconstruction, Modelling, and Statistical Approaches

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We are particularly interested in contributions, which elucidate the relationship between structure or dynamics of biological networks and biological function. This relationship may be observed on different scales, for example, on a global scale, or on the level of subnetworks or motifs.

Several levels exist on which to relate biological function to network structure. Given molecular biological interactions, networks may be analysed with respect to their structural and dynamical patterns, which are associated with phenotypes of interest. On the other hand, experimental profiles (e.g., time series, disturbances) can be used to reverse engineer network structures based on a model of the underlying functional network.

Is it possible to detect the interesting features with the current methods? And how is our picture of the relationship between network structure and biological function affected by the choice of methods?

Perspectives both from simulation approaches as well as the evaluation of experimental data and combinations thereof are welcome and will be integrated within this special issue.

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First Round of Reviews	September 1, 2008
Publication Date	December 1, 2008

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Special Issue on OFDMA Architectures, Protocols, and Applications

Call for Papers

Orthogonal frequency-division multiple access (OFDMA) technologies are currently attracting intensive attention in wireless communications to meet the ever-increasing demands arising from the explosive growth of Internet, multimedia, and broadband services. OFDMA-based systems are able to deliver high data rate, operate in the hostile multipath radio environment, and allow efficient sharing of limited resources such as spectrum and transmit power between multiple users. OFDMA has been used in the mobility mode of IEEE 802.16 WiMAX, is currently a working specification in 3GPP Long Term Evolution downlink, and is the candidate access method for the IEEE 802.22 “wireless regional area networks.” Clearly, recent advances in wireless communication technology have led to significant innovations that enable OFDMA-based wireless access networks to provide better quality-of-service (QoS) than ever with convenient and inexpensive deployment and mobility.

However, regardless of the technology used, OFDMA networks must not only be able to provide reliable and high quality broadband services, but also be implemented cost-effectively and be operated efficiently. OFDMA presents many of the advantages and challenges of OFDM systems for single users, and the extension to multiple users introduces many further challenges and opportunities, both on the physical layer and at higher layers. These requirements present many challenges in the design of network architectures and protocols, which have motivated a significant amount of research in the area. Also, many critical problems associated with the applications of OFDMA technologies in future wireless systems are still looking for efficient solutions. The aim of this special issue is to present a collection of high-quality research papers that report the latest research advances in this field from physical and network layers to practical applications. Original papers are solicited in all aspects of OFDMA techniques including physical layer issues, architectures, protocol designs, enabling technologies, theoretical studies, practical applications, and experimental prototypes. Topics of interest include, but are not limited to:

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- Signal processing for OFDMA
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- MAC and network layer management
- Cross-layer design and optimization
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- Quality of service provisioning
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Special Issue on Dependable Semantic Inference

Call for Papers

After many years of exciting research, the field of multimedia information retrieval (MIR) has become mature enough to enter a new development phase—the phase in which MIR technology is made ready to get adopted in practical solutions and realistic application scenarios. High users' expectations in such scenarios require high dependability of MIR systems. For example, in view of the paradigm “getting the content I like, anytime and anywhere” the service of consumer-oriented MIR solutions (e.g., a PVR, mobile video, music retrieval, web search) will need to be at least as dependable as turning a TV set on and off. Dependability plays even a more critical role in automated surveillance solutions relying on MIR technology to analyze recorded scenes and events and alert the authorities when necessary.

This special issue addresses the dependability of those critical parts of MIR systems dealing with semantic inference. Semantic inference stands for the theories and algorithms designed to relate multimedia data to semantic-level descriptors to allow content-based search, retrieval, and management of data. An increase in semantic inference dependability could be achieved in several ways. For instance, better understanding of the processes underlying semantic concept detection could help forecast, prevent, or correct possible semantic inference errors. Furthermore, the theory of using redundancy for building reliable structures from less reliable components could be applied to integrate “isolated” semantic inference algorithms into a network characterized by distributed and collaborative intelligence (e.g., a social/P2P network) and let them benefit from the processes taking place in such a network (e.g., tagging, collaborative filtering).

The goal of this special issue is to gather high-quality and original contributions that reach beyond conventional ideas and approaches and make substantial steps towards dependable, practically deployable semantic inference theories and algorithms.

Topics of interest include (but are not limited to):

- Theory and algorithms of robust, generic, and scalable semantic inference
- Self-learning and interactive learning for online adaptable semantic inference

- Exploration of applicability scope and theoretical performance limits of semantic inference algorithms
- Modeling of system confidence in its semantic inference performance
- Evaluation of semantic inference dependability using standard dependability criteria
- Matching user/context requirements to dependability criteria (e.g., mobile user, user at home, etc.)
- Modeling synergies between different semantic inference mechanisms (e.g., content analysis, indexing through user interaction, collaborative filtering)
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First Round of Reviews	February 1, 2009
Publication Date	May 1, 2009

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Special Issue on Game Theory in Signal Processing and Communications

Call for Papers

Game theory is a branch of mathematics aimed at the modeling and understanding of rational behavior in strategic situations. In the last decade, game theory has been applied to solve conflict problems in economics, and has found important applications in politics, sociology, psychology, and transportation. Game theory has more recently been employed to model and analyze modern communication systems, such as power control in wireless networks and routing in wire line networks. Also, it provides a structured approach to many important signal processing problems, including cognitive radio, waveform design, and dynamic spectrum access. Game theory is successfully applied to design decentralized algorithms and robust signal processing methods in various deployment scenarios.

This special issue aims to promote the field of game theory to the signal processing audience. We are soliciting high-quality unpublished research papers addressing the theory and practice of game theory in signal processing and communications. Topics include, but are not limited to:

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- Cooperative (bargaining) game theory
- Auctions, coalitions, and pricing
- Game theory for resource allocation in communications
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Manuscript Due	October 1, 2008
First Round of Reviews	January 1, 2009
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Special Issue on Advances in Propagation Modelling for Wireless Systems

Call for Papers

The true challenge for new communication technologies is to “make the thing work” in real-world wireless channels. System designers classically focus on the impact of the radio channel on the received signals and use propagation models for testing and evaluation of receiver designs and transmission schemes. Yet, the needs for such models evolve as new applications emerge with different bandwidths, terminal mobility, higher carrier frequencies, new antennas, and so forth. Furthermore, channel characterization also yields the fundamental ties to classical electromagnetics and physics, as well as the answers to some crucial questions in communication and information theory. In particular, it is of outstanding importance for designing transmission schemes which are efficient in terms of power or spectrum management.

The objective of this special issue is to highlight the most recent advances in the area of propagation measurement and modeling. Original and research articles are solicited in all aspects of propagation, including experimental characterization, channel sounding, theoretical modeling, hardware emulation and new communication technologies.

Topics include, but are not limited to:

- 4G channel measurements and modeling
- Fixed wireless access (including outdoor-to-indoor)
- UWB propagation
- 60 GHz channel measurements and modeling
- Propagation models for wireless sensor networks, including RFIDs
- Spectrum sensing and channel prediction for cognitive radio
- Intra/inter vehicle and vehicle-to-infrastructure channel characterization
- Body area propagation modeling
- Double-directional and MIMO channels
- Multiuser MIMO channels
- Multi-hop and cooperative channels
- Polarimetric channels
- Shadowing correlation modeling
- Temporal variations in wireless channels
- Frequency and range dependence of parameters

- High-resolution algorithms for parameter extraction
- Channel prediction and tracking
- Numerical methods in wireless channel modeling
- Advances in channel emulation and sounding

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Manuscript Due	August 1, 2008
First Round of Reviews	November 1, 2008
Publication Date	February 1, 2009

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ISSN: 1687-6911; e-ISSN: 1687-692X; doi:10.1155/RLSP

Hindawi Publishing Corporation

410 Park Avenue, 15th Floor, #287 pmb, New York, NY 10022, USA

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SIGNAL PROCESSING

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Volume 2007

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